

F2

Addition

Vocabulary: subitise, number, numeral, composition, whole/part/part, number bonds, double, and, add, plus, equals, altogether, total, count on

Concrete

Pictorial

Abstract

Composition of numbers

Children talk about the different arrangements they can see within a whole.
Play games e.g., skittles and looking at how many are standing. How many have fallen over? How many are there altogether?



Show children pictures of the skittles. Can children identify the two parts?



How can they show it? Circle.

Draw it.



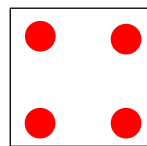
No formal written method.

Child can record the abstract as a number sentence for example:
 $3 + 3 = 6$

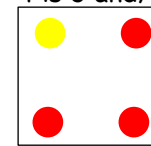
They could record as pictures, bar model or in a part whole model.

Exploring a number

How many different ways can we make 4? What is different? What is the same?

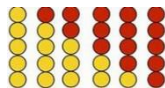


4 is 3 and +1

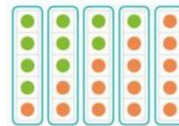


Systematic working and commutativity (counters/cubes)

Ways to make numbers to 5.



Ways to make numbers to 5

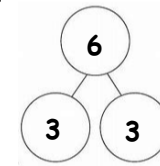


Exploring numbers using Maths equipment (Numicon/rekenrek)



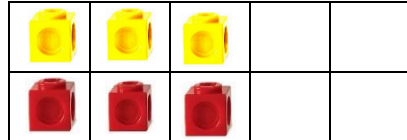
Jottings

4 and 1 = 5



frames and 10 frames.

$3 + 3$



Jottings

$3 + 3$



Conceptual subitising

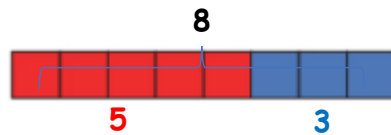
Recognising smaller groups within a larger set and adding those small groups together, such as 2 dots plus 2 dots equals four dots.



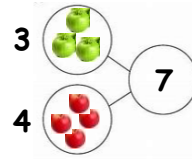
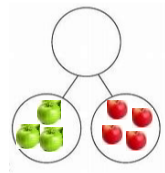
$2 + 2 = 4$



Bar model



Joining two groups and counting all.



Tell a number story to match a picture.
The boy has 3 green apples, and the girl has 4 red apples. Altogether they have 7 apples.



Instant Recall

- Number bonds to 5
- Some number bonds to 10

Mental

Encourage children to visualise a hidden group and calculate how many altogether for example there are 3 apples in the bowl, there are 4 apples next to the bowl, how many apples altogether? 3 plus 4 equals... how do you know? Convince me.

YEAR 1

Addition

Vocabulary: Addition, add, forwards, put together, more than, total, altogether, equals, same as, greater than, most, pattern, odd, even, digit, counting on, part, whole.

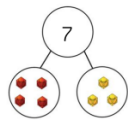
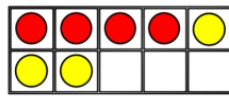
Concrete

Add numbers within 10 including number bonds to 10

$4 + 3 = 7$
 $3 + 4 = 7$



$7 = 4 + 3$



$7 = 4 + 3$
 $7 = 3 + 4$

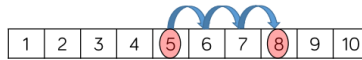
Plus using place value mats and diennes.

Pictorial

Add numbers within 10 including number bonds to 10

Number line (counting on):

$5 + 3 = 8$

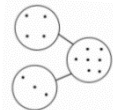


Diennes jottings:

$5 + 3 = 8$



Part part whole model:



$7 = 4 + 3$
 $7 = 3 + 4$

Abstract

Mental facts to 10

Number facts

Recall and use addition facts to 10 fluently
the total of 6 and 3 6 plus 2 4 more than 5

Near doubles:

Instantly recall doubles to 10 and use this to calculate near doubles.

$4 + 5 = 4 + 4 + 1$ OR

$4 + 5 = 5 + 5 - 1$

One and two more:

Of numbers up to 10.

$8 + 1 = 9$ (consecutive numbers)

$5 + 2 = 7$ (Consecutive odd or even numbers)

$4 + 2 = 6$

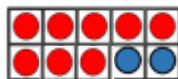
Number bonds to 10:

$8 + 2 = 10$

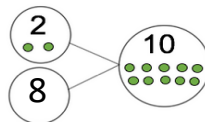
Numicon



10 frame



Number bonds to 10:



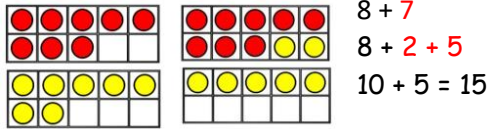
Instant recall of facts

Number bonds to 10:

- $0 + 10 = 10$
- $1 + 9 = 10$
- $2 + 8 = 10$
- $3 + 7 = 10$
- $4 + 6 = 10$
- $5 + 5 = 10$
- $6 + 4 = 10$
- $7 + 3 = 10$
- $8 + 2 = 10$
- $9 + 1 = 10$
- $10 + 0 = 10$

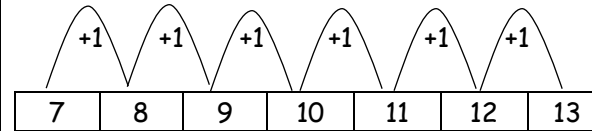
Add numbers within 20 including number bonds to 20:

Partitioning:



Add numbers within 20 including number bonds to 20:

Partitioning: $7 + 6$



Moving on to partitioning 6 into 3 and 3
 ($7 + 3 = 10$ then $10 + 3 = 13$)

Mental facts to 20

Partitioning (bridging through 10):

$5 + 7$
 $5 + 5 + 2$ (partition 7 into 5 and 2) OR
 $7 + 3 + 2$ (partition 5 into 3 and 2)

Using known facts and place value

$15 + 4$
 $5 + 4 = 9$ so $15 + 4 = 19$

Number facts

Know number pairs with a total of 20
 $16 + \square = 20$ $20 = 3 + \square$

One and two more:

Of numbers up to 20.
 $18 + 1 = 19$ (consecutive numbers)
 $15 + 2 = 17$ (Consecutive odd or even numbers)
 $14 + 2 = 16$

Instant recall of facts:

Number bonds to 20

Redistribution:

$12 + 5$ redistributes to $10 + 7$.

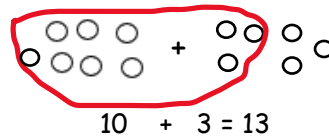
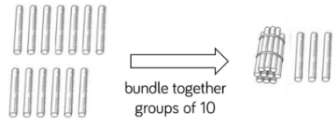
Commutativity and Inverse

$16 + 4 = 20$ $20 - 16 = 4$
 $4 + 16 = 20$ $20 - 4 = 16$

Missing Number/Inverse

$\square - 5 = 12$ $12 - \square = 4$

$7 + 6 = 13$



Counting on:



Number bonds to 20:

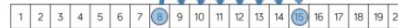
$16 + 4 = 20$
 $4 + 16 = 20$

Cubes

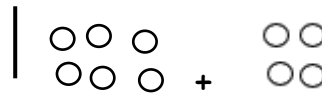


Counting on:

$8 + 7 = 15$



Number bonds to 20:



YEAR 2

Addition

Vocabulary:

Addition, add, plus, altogether, count on, equals, in total, in all, same as, whole, part, number bonds, number sentence, calculation, number, numeral, digit (one-digit, two-digit), odd, even, pattern, tens, ones, partition, commutativity, jottings. (see previous year groups)

Concrete

Pictorial

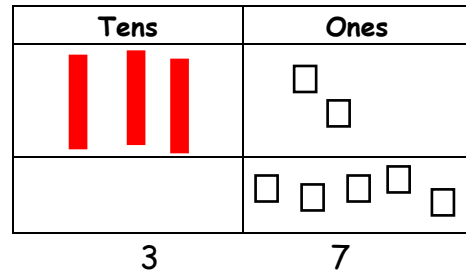
Abstract

Children need to be secure in number bonds to 10 and 20. See Year 1 addition policy.

Adding 2 digit numbers + multiples of 1 and 10

No exchanging (diennes)

$32 + 5 = 37$ or $5 + 32 = 37$



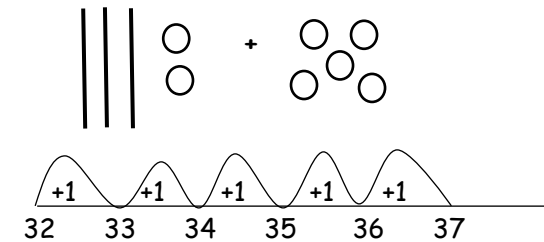
Leading onto a 2-digit number add tens ($34 + 40$)

Linear?

Adding 2 digit numbers + multiples of 1 and 10

No exchanging

$32 + 5 = 37$ or $5 + 32 = 37$



Then adding tens only.

Adding 2 digit numbers + multiples of 1 and 10

No exchanging

Adding ones

Adding tens

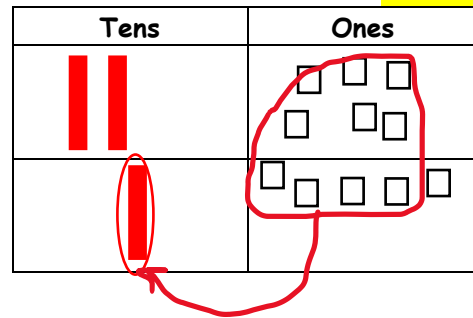
T	O
3	2
+	5
3	7

Tens	Ones
3	2
2	0
5	0

This written method is only shown alongside the pictorial.

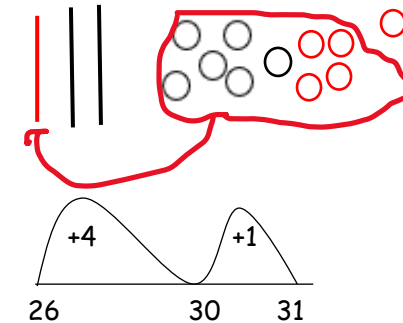
Exchanging (diennes)

$26 + 5 = 31$ or $5 + 26 = 31$ Linear?



Exchanging

$26 + 5 = 31$ or $5 + 26 = 31$




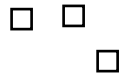


No written method for exchanging.

Adding two 2 digit numbers

No exchanging

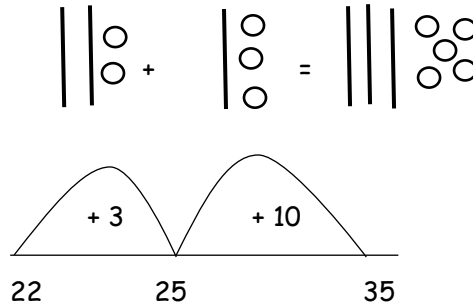
$22 + 13 = 35$ Linear?

Tens	Ones
	
	

Adding two 2 digit numbers

No exchanging

$22 + 13 = 35$



Written

Adding two 2 digit numbers

No exchanging


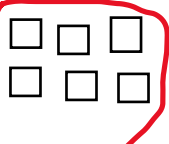
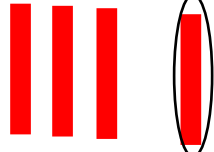
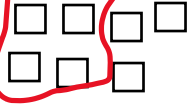
Tens	Ones
2	2
1	3
	5
3	0
3	5

Tens	Ones
2	2
1	3
3	5

This written method is only shown alongside the pictorial representation.

Exchanging

$26 + 37 = 63$

Tens	Ones
	
	

6

3

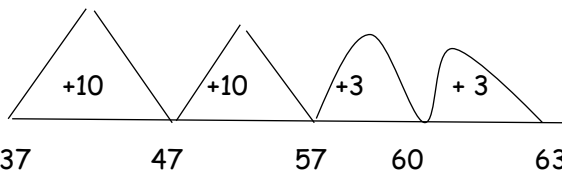
Linear?

Exchanging

$26 + 37 = 63$

63	
26	37

Using a number line



(children may count in ones from 57 to 63 to start with).

Change to adding ones first

No written method for exchanging.

Mental Methods

Number facts:

Known complements to the next multiple of 10

$$52 + \underline{\quad} = 60$$

Know pairs of multiples of 10 totalling 100

$$60 + \underline{\quad} = 100$$

Number bonds to 10:

$$46 + 4 = 50 \quad (6 + 4 = 10)$$

Counting on:

$$37 + 20 \text{ (+10 then +10)}$$

$$42 + 23 \text{ (+20 then +3)}$$

$$47 + 15 \text{ (+10, +3 to the next 10 then +2)}$$

Near doubles:

$$\text{If } 7 + 7 = 14$$

$$\text{Then } 7 + 8 = 14 + 1 = 15$$

Redistribution:

$$38 + 47$$

$$\text{Redistribute to } 40 + 45 = 95$$

Partitioning:

$$23 + 12$$

$$20 + 10 = 30; 3 + 2 = 5; 30 + 5 = 35$$

Adjusting:

$$34 + 9 \text{ (+10 then subtract 1)}$$

$$45 + 19 \text{ (+20 then subtract 1)}$$

Using known facts and place value:

$$63 + 4$$

$$\text{If } 3 + 4 = 7 \text{ then } 63 + 4 = 67$$

$$40 + 50$$

$$\text{If } 4 + 5 = 9 \text{ then } 40 + 50 = 90$$

Inverse:

Understand the inverse:

$$45 + 8 = 53$$

$$8 + 45 = 53$$

$$53 - 45 = 8$$

$$53 - 8 = 45$$

YEAR 3

Addition

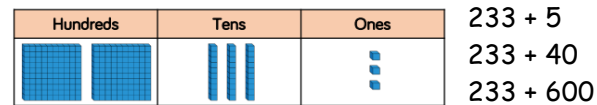
Vocabulary:

Hundreds, tens, ones, estimate, partition, recombine, difference, decrease, near multiple of 10 and 100, inverse, rounding, column subtraction, exchange. (see previous year groups)

Concrete

Adding 100s, 10s and 1s no exchanging:

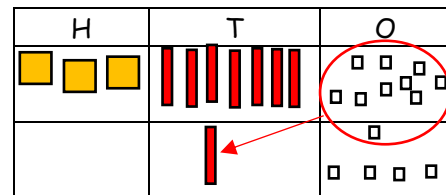
(Use diennes, place value counters or numicon).



Initially add 1, 10 and 100 before moving onto adding multiples of 1, 10 and 100.

Adding 100s, 10s and 1s exchanging:

$$379 + 5 = 384$$

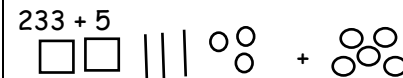


(for $379 + 40$ then 10 tens = 1 hundred)

Pictorial

Adding 100s, 10s and 1s no exchanging:

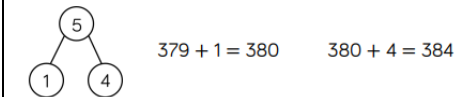
Use diennes notation:



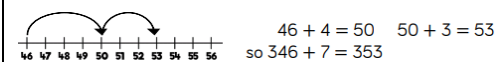
Adding 100s, 10s and 1s exchanging:

Partitioning:

$$379 + 5 = 384$$

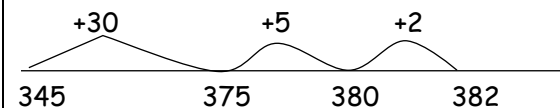


$$346 + 7 = 353$$



$$345 + 37 = 382$$

(Partitioning the second number and counting on)



Abstract

Mental

Counting On

$$137 + 50$$

(counting on in tens; 147, 157, 167, 177)

Adjusting:

$$234 + 29 \text{ (add 30 and subtract 1)}$$

$$234 + 99 \text{ (add 100 and subtract 1)}$$

$$234 + 299 \text{ (add 300 and subtract 1)}$$

Using Known Facts And Place Value:

$$282 + 7$$

$$2 + 7 = 9 \text{ so } 282 + 7 = 289$$

$$231 + 50$$

$$30 + 50 = 80 \text{ so } 231 + 50 = 281$$

Partitioning:

$$236 + 133$$

$$200 + 100 = 300$$

$$30 + 30 = 60$$

$$6 + 3 = 9,$$

$$\text{So } 300 + 60 + 9 = 369$$

Redistribution:

$$136 + 47 \text{ redistribute to } 133 + 50 = 183$$

Adding 3-digit numbers:

Starting with no exchanging leading onto exchanging in the ones then the tens then the ones AND tens.

Diennes:

Hundreds	Tens	Ones

265
+ 164
9
120
300
429

Place Value Counters:

Hundreds	Tens	Ones

384
+ 237
11
110
500
621

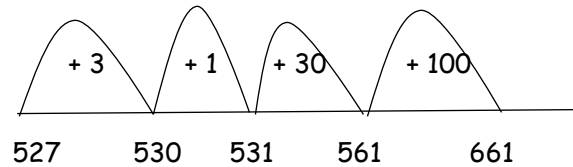
Adding 3-digit numbers:

?	
265	164

Use diennes jottings for adding where:

= 100 = 10 = 1

527 + 134 = 661



Written

Add numbers with up to 3 digits

No exchanging:

$\begin{array}{r} 322 \\ + 235 \\ \hline 7 \\ 50 \\ \hline 500 \\ 557 \end{array}$	$\begin{array}{r} 322 \\ + 235 \\ \hline 557 \end{array}$
--	---

Exchanging:

Ones to tens	Tens to hundreds
$\begin{array}{r} 527 \\ + 134 \\ \hline 11 \\ 50 \\ \hline 600 \\ 661 \end{array}$	$\begin{array}{r} 362 \\ + 451 \\ \hline 3 \\ 110 \\ \hline 700 \\ 813 \end{array}$

YEAR 4

Addition

Vocabulary:

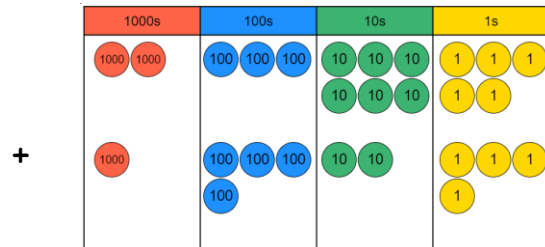
thousands, hundreds, tens, ones, estimate, partition, recombine, increase, near multiple of 10 and 100, inverse, rounding, column addition, exchange, addend + addend = sum/total (See previous year groups)

Concrete

Add whole numbers with up to 4 digits.

No exchanging:

$2365 + 1424 = 3789$

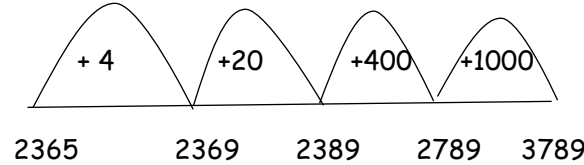


Pictorial

Add whole numbers with up to 4 digits.

No exchanging:

$2365 + 1424 = 3789$



Abstract

Written

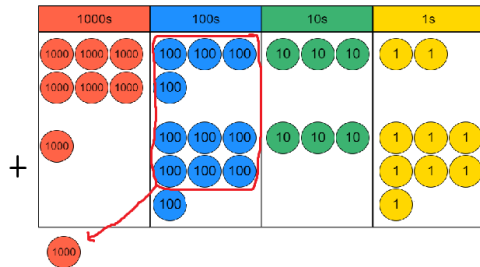
Add whole numbers with up to 4 digits.

No exchanging:

$$\begin{array}{r} 2365 \\ + 1424 \\ \hline 3789 \end{array}$$

Exchanging:

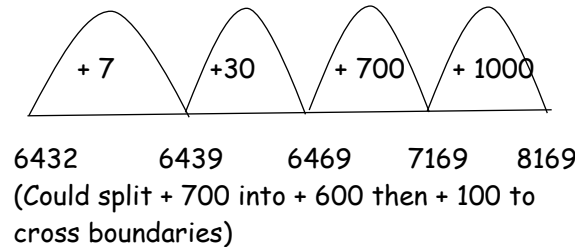
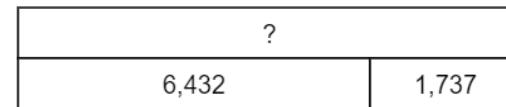
$6,432 + 1,737 = 8169$



Start without exchanging leading onto exchanging at different points (ones to tens; tens to hundreds etc).

Exchanging:

$6432 + 1737 = 8169$



Exchanging:

Expanded















$$\begin{array}{r} \text{Th H T O} \\ 6 \ 432 \\ + 1 \ 737 \\ \hline 9 \\ 60 \\ 1 \ 100 \\ 7 \ 000 \\ \hline 8 \ 169 \end{array}$$

Compact

$$\begin{array}{r} \text{Th H T O} \\ 6 \ 432 \\ + 1 \ 737 \\ \hline 8 \ 169 \\ \hline 1 \end{array}$$

Add decimals up to 2 decimal places (as money or measures):

$$£15.54 + £26.25 = £41.79$$

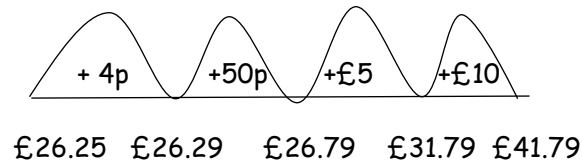
T	O	th	hth
	 		 
	 	  	 

Use place value counters or money depending on the context.

Start with no exchanging leading to exchanging.

Add decimals up to 2 decimal places (as money or measures):

$$£15.54 + £26.25 = £41.79$$



Add decimals up to 2 decimal places (as money or measures):

Expanded	Compact
£26.25	£26.25
+ £15.54	+ £15.54
<hr/>	<hr/>
0.09	£41.79
0.70	1
11.00	
<hr/>	
30.00	
<hr/>	
£41.79	

Mental Methods:

Counting on:

$$2534 + 2150$$

$$2534 + 2000 + 100 + 50 = 4684$$

Using known facts and place value:

$$5060 + 47$$

$$60 + 47 = 107 \text{ so } 5060 + 47 = 5107$$

$$0.6 + 0.2$$

$$\text{If } 6 + 2 = 8 \text{ then } 0.6 + 0.2 = 0.8$$

Redistribution:

$$2504 + 3234 \text{ redistribute to } 2500 + 3238.$$

Adjusting:

Demo on a number line first.

$$2345 + 499 \text{ (add 500 and subtract 1)}$$

$$2345 + 2999 \text{ (add 3000 and subtract 1)}$$

Partitioning:

$$2314 + 1242$$

$$2000 + 1000 = 3000$$

$$300 + 200 = 500$$

$$10 + 40 = 50$$

$$4 + 2 = 6$$

$$3000 + 500 + 50 + 6 = 3556$$

YEAR 5

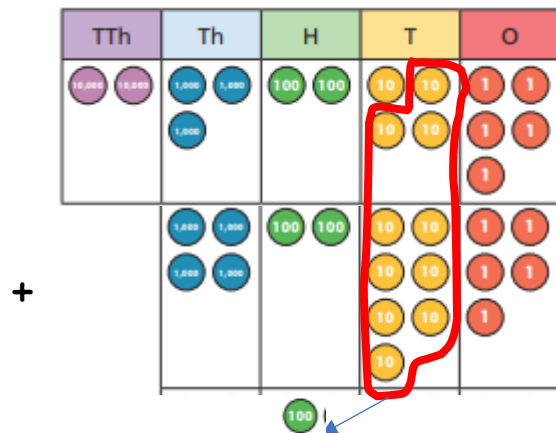
Addition

Vocabulary: sum, total, parts and whole, plus, add, altogether, more than; addend + addend = sum/total (see previous year groups)

Concrete

Add whole numbers with more than 4 digits.
(Up to answers with 6 digits).

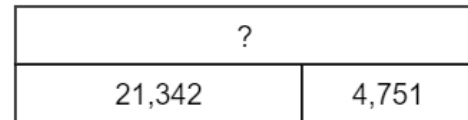
$$21\ 342 + 4\ 751 = 26\ 093$$



Pictorial

Add whole numbers with more than 4 digits.

$$21\ 342 + 4\ 751 = 26\ 093$$



Abstract

Written

Add whole numbers with more than 4 digits.

Exchanging

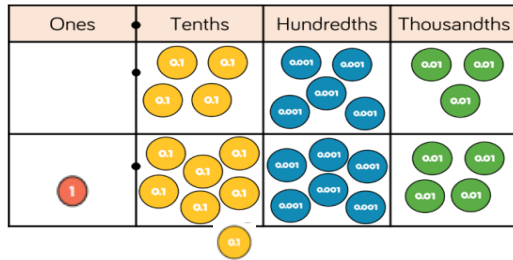
(building up from non exchanging then exchanging at diferent points)

$$21\ 342 + 4\ 751 = 26\ 093$$

	TTh	Th	H	T	O
	2	1	3	4	2
+		4	7	5	1
	2	6	0	9	3
					1

Adding decimals (up to 3 decimal places)

$0.453 + 0.664 = 1.117$

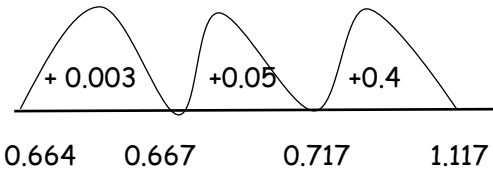
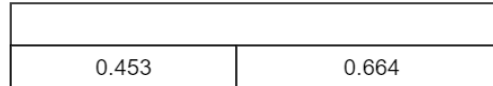


1 . 1 1 7

Start with no exchanging then build up by exchanging at different points.

Adding decimals (up to 3 decimal places)

$0.453 + 0.664 = 1.117$



Adding decimals (up to 3 decimal places)

$0.453 + 0.664 = 1.117$

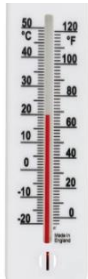
Exchanging

(building up from non exchanging then exchanging at different points)

$$\begin{array}{r}
 0.453 \\
 + 0.664 \\
 \hline
 1.117 \\
 1 \quad 1
 \end{array}$$

Adding negative numbers

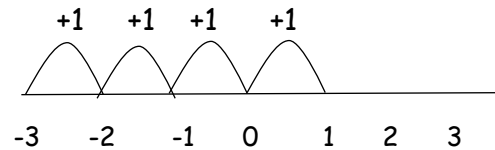
Using real life objects:



Adding negative numbers

Using a number line (the number line could be represented vertically too):

$-3 + 4 = 1$



Adding negative numbers

Develops into a mental method - no written method.

Mental Methods:

Counting on:

$4.3 + 1.5$

(partition 1.5 then +1 and + 0.5)

$19.7 + 2.6$

(+2, +0.3 to the next whole number then +0.3)

Redistribution:

$0.66 + 0.23$ redistribute to $0.69 + 0.20$

Adjusting:

$2\,456 + 399$ (add 400 and subtract 1)

$8.3 + 1.9$ (add 2 and subtract 0.1)

$14.6 + 3.9$ (add 4 and subtract 0.1)

Using known facts and place value:

$7.5 + 2.6$

$7.5 + 2.5 = 10$ so $7.5 + 2.6 = 10.1$

$0.06 + 0.08$

If $6 + 2 = 8$ then $0.06 + 0.02 = 0.08$

Derive and use addition facts to 1 (with decimals up to 2 decimal places).

Recall and use addition facts for 1 and 10 (with decimal numbers up to 1 place)

Recall pairs of 3 digit numbers with a total of 1000.

Partitioning:

Adding a power of 10

$23\,453 + 10\,000 = 33\,453$

$45\,321 + 1\,000 = 46\,321$

No exchanging

$42\,345 + 21\,423 = 63\,768$

Exchanging

$3.6 + 1.7$

$3 + 1 = 4$

$0.6 + 0.7 = 1.3$

$4 + 1.3 = 5.3$

YEAR 6

Addition

Vocabulary: sum, total, parts and whole, plus, add, altogether, more than; addend + addend = sum/total (see previous year groups)

Concrete

Add larger whole numbers.

$$6,537,206 + 1,374,023 = 7\,911\,229$$

Millions	Hundred Thousands	Ten Thousands	Thousands	Hundreds	Tens	Ones
+						
7	9	1	1	2	2	9

No place value counters for larger numbers. Revisit previous years' addition calculation policies.

Pictorial

Add larger whole numbers

Number lines from previous year groups are used if needed.

Abstract

Add larger whole numbers (exchanging at different points)

$$\begin{array}{r}
 \text{M HTh TTh Th H T O} \\
 6\ 5\ 3\ 7\ 2\ 0\ 6 \\
 + 1\ 3\ 7\ 4\ 0\ 2\ 3 \\
 \hline
 7,\ 9\ 1\ 1,\ 2\ 2\ 9 \\
 \text{\small } \swarrow \quad \swarrow
 \end{array}$$

Adding decimals up to 3 decimal places.

(including decimals with different numbers of decimal places)

Ones	Tenths	Hundredths	Thousandths

Adding decimals up to 3 decimal places.

(including decimals with different numbers of decimal places)

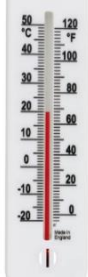
See previous addition policies if needed for jottings using a number line.

Adding decimals up to 3 decimal places
(including decimals with different numbers of decimal places)

$$\begin{array}{r}
 \text{O . t h th} \\
 0 . 4 5 3 \\
 + \underline{0 . 6 6 4} \\
 \hline
 1 . 1 1 7 \\
 \text{\small } \swarrow \quad \swarrow
 \end{array}$$

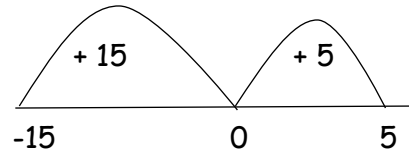
Adding negative numbers

In real life contexts



Adding negative numbers

$$-15 + 20 = 5$$



(could go up in 1s first)

Adding negative numbers

Develops into a mental method - no written method.

Mental

Counting on:

$$6.46 + 2.03$$

(partition 2.03 then +2 and +0.03)

Adjusting:

$$34\,256 + 14\,999 \text{ (add 15\,000 and subtract 1)}$$

$$6.73 + 0.99 \text{ (add 1 and subtract 0.01)}$$

Using known facts and place value:

$$0.64 + 0.36$$

$$64 + 36 = 100 \text{ so } 0.64 + 0.36 = 1$$

Partitioning:

Adding a power/multiple of 10

$$163\,453 + 20,000$$

$$275\,321 + 1,000$$

(children recognise which column will change)

No exchanging

$$345\,252 + 223\,516$$

$$3.421 + 2.357$$

Exchanging

$$3.4 + 2.77$$

$$3 + 2 = 5$$

$$0.4 + 0.7 = 1.1$$

$$5 + 1.1 + 0.07 = 6.17$$